

Atlantic Hurricane Statistical Analysis

Read Atlantic Storm Re-analysis Data from 1851 to 2004 from National Hurricane Center

Data: Line#, Mon, Day, Yr, Duration, NumYr, Num, Name, Land, SSS, XXX, Vel, Press, Line#, Type, Lat, Long

SD :=

1851-2004r.xls

Number of Data Type Columns

$C := \text{cols}(SD) - 1$

Extract Wind Velocity (Knots) and Pressure (mb) Data

Velocity := SD⁽¹¹⁾

Pressure := SD⁽¹²⁾

max(Velocity) = 165

Group Data by Wind Speed: Hurricanes (V > 63 Knots) and Cat 3 (V > 95Knots) and Greater

CSSD := csort(SD, 11)

match(65, CSSD⁽¹¹⁾)₀ = 517

match(95, CSSD⁽¹¹⁾)₀ = 1007

Sort by Land Fall

CSLF := csort(SD, 8)

match(1, CSLF⁽⁸⁾)₀ = 816

Sort by Storm Number (Year)

HCSSD := submatrix(CSSD, 514, 1300 - 1, 0, C)

HDY := csort(HCSSD, 6)

H3SSD := submatrix(CSSD, 1004, 1300 - 1, 0, C)

H3Y := csort(H3SSD, 6)

HLFSD := submatrix(CSLF, 813, 1300 - 1, 0, cols(CSLF) - 1)

HLF := csort(HLFSD, 6)

YearS := SD⁽³⁾

YearH := HDY⁽³⁾

Year3 := H3Y⁽³⁾

YearLF := HLF⁽³⁾ YearS₀ = 1851

TS := histogram(154, YearS)

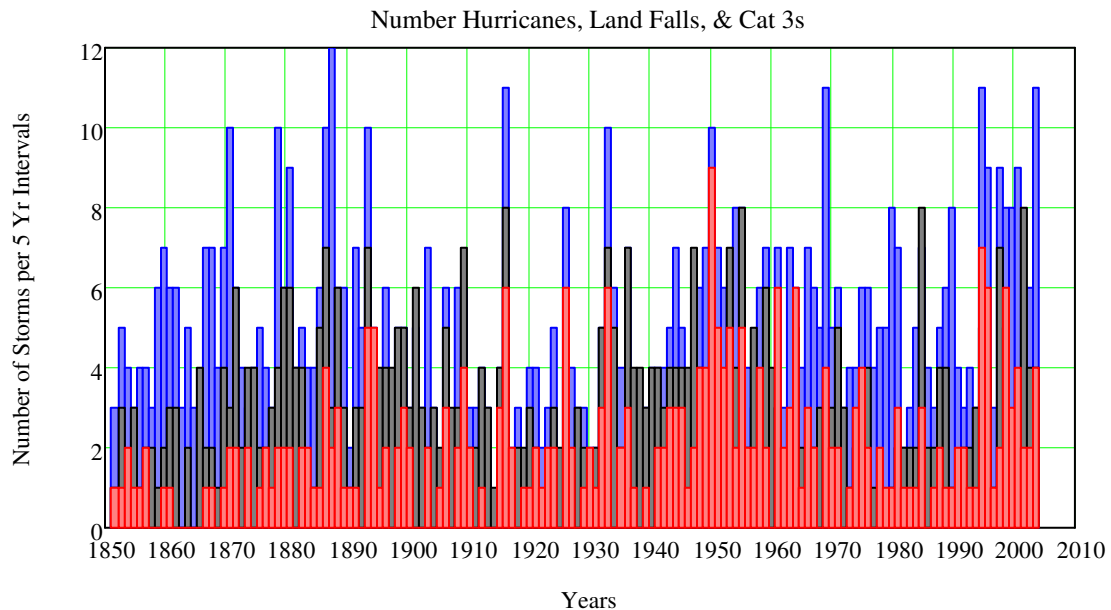
2004 - 1851 = 153

$H := \text{histogram}(154, \text{YearH})$

H3 := histogram(154, Year3)

LF := histogram(154, YearLF)

Plot the Number of: Hurricanes (H), Hurricanes with Land Falls (LF) and Cat 3 Hurricanes (H3)



Plot Histograms of Wind Velocity and Pressure at Eye Wall

VD := histogram(20, Velocity) CSP := csort(HDY, 12) rows(SD) = 1321

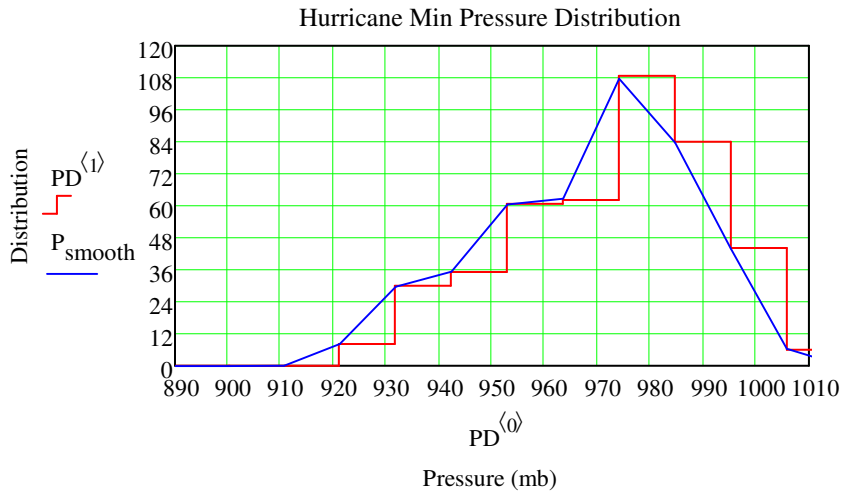
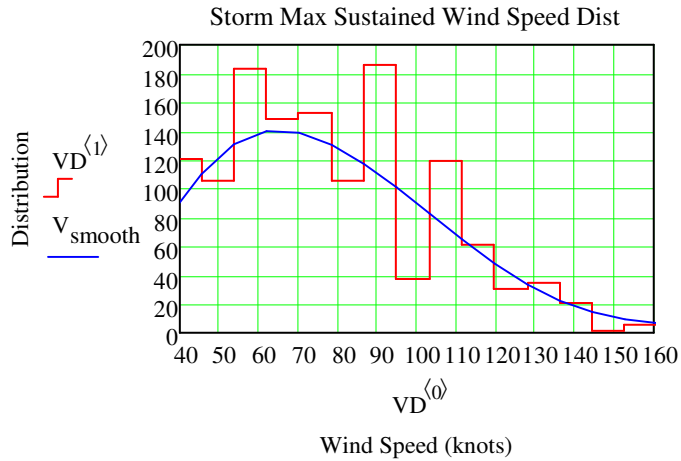
match(9999, CSP⁽¹²⁾)₀ = 442

PSS := submatrix(CSP, 0, 445 - 1, 0, C) max(PSS⁽¹²⁾) - min(PSS⁽¹²⁾) = 9929

PD := histogram(939, PSS⁽¹²⁾)

Smooth Discrete Data

P_{smooth} := ksmooth(PD⁽⁰⁾, PD⁽¹⁾, 10) V_{smooth} := ksmooth(VD⁽⁰⁾, VD⁽¹⁾, 40)



Select Most Reliable (Recent) Storm Data from 1900 to 2004

Lines 370 and 1235 are the start of 1900 and end of 2000 rows(SD) = 1321

Sd := submatrix(SD, 370, 1318 - 1, 0, C) match(1900, SD⁽³⁾)₀ = 370

HDY⁽⁸⁾ := $\overrightarrow{(HDY^{(8)} - 100000 - HDY^{(8)})}$ match(2001, SD⁽³⁾)₀ = 1262

Find the Start Date of Storms in Days from Beginning of Year
Months per day and Total from Jan to Dec

MonthDays := (0 31 28 31 30 31 30 31 31 30 31 30 31)^T

MonthDayTotals := (0 31 59 90 120 151 181 212 243 273 304 334 365)^T

Month := Sd⁽¹⁾ Day := Sd⁽²⁾ Duration := Sd⁽⁴⁾

N := rows(Month) n := 0..N - 1 SNBR := Sd⁽⁶⁾

Start_n := MonthDayTotals_{Month_n-1} + Day_n Start_Sd := Sd⁽¹⁵⁾

Range := max(Start) - min(Start) Range = 346

H_{start} := histogram(Range + 1, Start) Min Between Peaks is 261 Days

h_{start} := ksmooth(H_{start}⁽⁰⁾, H_{start}⁽¹⁾, 5) MonthDayTotals₈ + 18 = 261

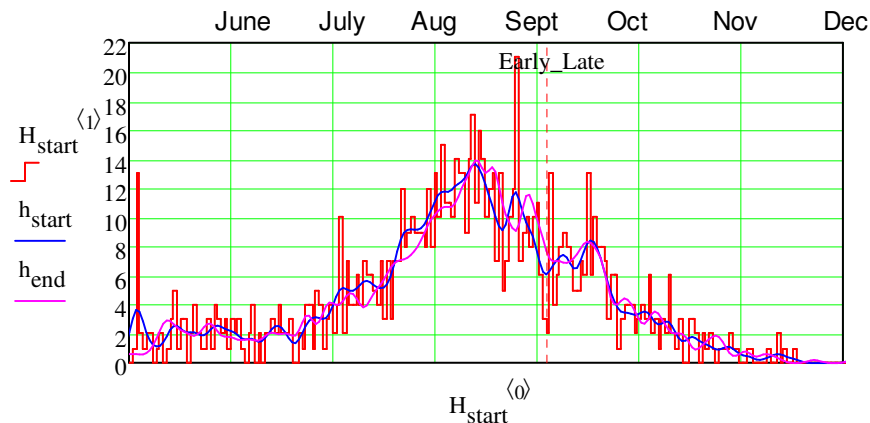
End := $\overrightarrow{(Start + Duration)}$ Min Between Peaks is Sept 18th

H_{end} := histogram(Range + 1, End)

h_{end} := ksmooth(H_{end}⁽⁰⁾, H_{end}⁽¹⁾, 5) Early_Late := 273

Plot Start and End Dates of All Storms

Note that there are two peaks (Sept 6 and Sept 21) indicating two different major factors
(The dividing date for the smoothed curve appears to be at 273 days or Oct 1st)



Hurricanes Only 1900 - 2004: Plot Start and End Dates

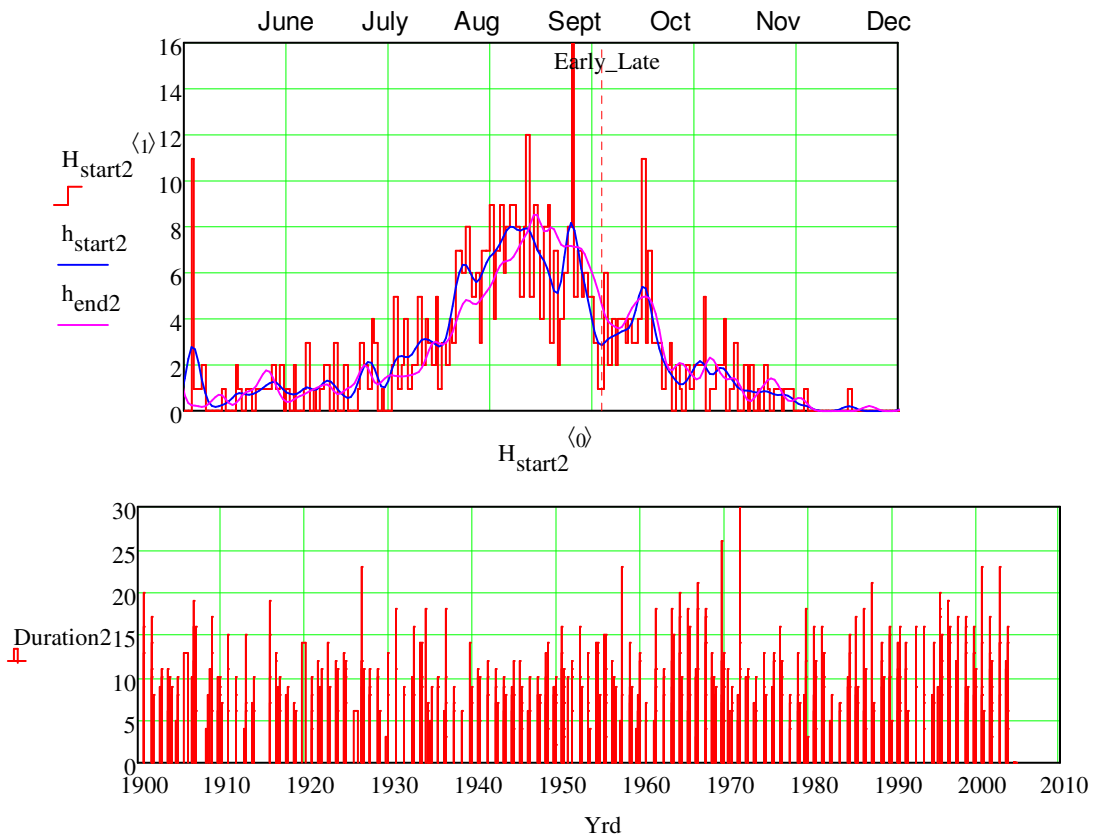
```

Hdd := submatrix(HDY, 261, rows(HDY) - 1, 0, cols(HDY) - 1)  Yr := Hdd<3>

Month2 := Hdd<1>          Day2 := Hdd<2>          Duration2 := Hdd<4>
N := rows(Day2)          n := 0..N - 1          SNBR := Hdd<6>
Start2_n := MonthDayTotals_Month2_n-1 + Day2_n          rows(Start) = 948
Range2 := max(Start2) - min(Start2)          Range2 = 299
H_start2 := histogram(Range2 + 1, Start2)          End2 := (Start2 + Duration2)
h_start2 := ksmooth(H_start2<0>, H_start2<1>, 5)          rows(Start) = 948
H_end2 := histogram(Range2 + 1, End2)          rows(Duration2) = 525
h_end2 := ksmooth(H_end2<0>, H_end2<1>, 5)          DurationDays_Avg := mean(Duration2)
DurationDays_Avg = 9.531
Yrd := (Yr + Start2*0.003)
    
```

Plot Start and End Dates and Duration of Hurricanes

Note that there are two peaks (Sept 6 and Oct 21) indicating two different major factors



Separate Hurricanes into those before and after Days = 273 (Oct 1st)

$HddS := \text{csort}(Hdd, 15)$ $R := (\text{rows}(Hdd) - 1)$ $Date := HddS^{(15)}$
 $Hdd_{Early} := \text{submatrix}(HddS, 0, 391, 0, C)$ $Hdd_{Late} := \text{submatrix}(HddS, 392, R, 0, C)$
 $LandFall_{Early} := Hdd_{Early}^{(8)}$ $LandFall_{Late} := Hdd_{Late}^{(8)}$
 $Lat_{Early} := 0.1 \cdot Hdd_{Early}^{(16)}$ $Lat_{Late} := 0.1 \cdot Hdd_{Late}^{(16)}$
 $LatLF_{Early} := \overrightarrow{(LandFall_{Early} \cdot Lat_{Early})}$ $LatLF_{Late} := \overrightarrow{(LandFall_{Late} \cdot Lat_{Late})}$
 $Long_{Early} := -0.1 \cdot Hdd_{Early}^{(17)}$ $Long_{Late} := -0.1 \cdot Hdd_{Late}^{(17)}$

Find the Fraction of Hurricanes that are Early and Late

$$\frac{\text{rows}(Hdd_{Early})}{\text{rows}(HddS)} = 0.747$$

$$\frac{\text{rows}(Hdd_{Late})}{\text{rows}(HddS)} = 0.253$$

Find the Fraction of Each Type of Hurricane that Makes Land Fall in USA

$$\text{mean}(\Phi(LandFall_{Early})) = 0.401$$

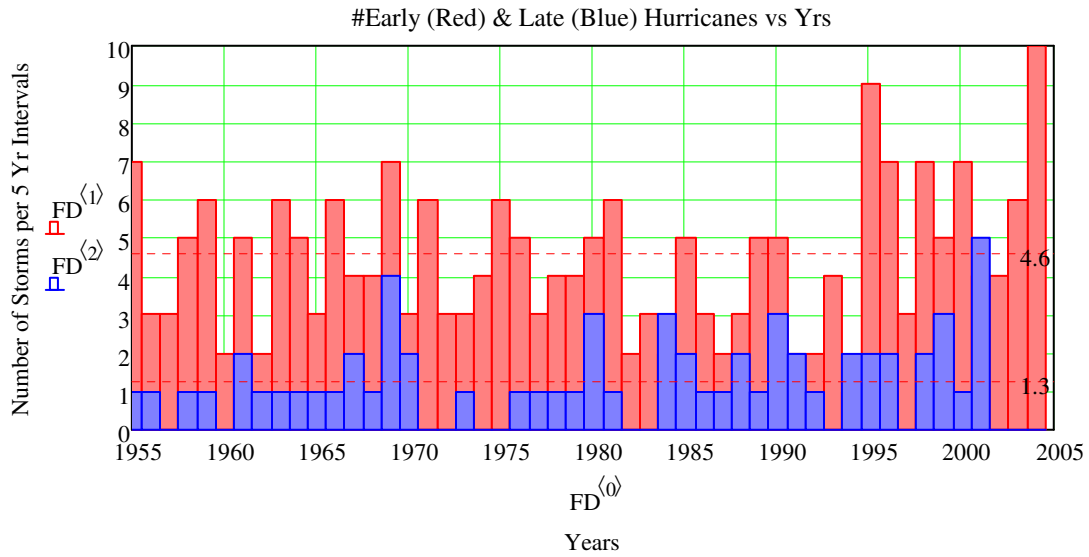
$$\text{mean}(\Phi(LandFall_{Late})) = 0.271$$

Find correlation between the Yearly Occurrence Frequency of Early and Late Hurricanes

Note There were no hurricanes in 1907 and 1914

$ELF(M) :=$

$y \leftarrow 0$ $r \leftarrow 0$ while $r < \text{rows}(M) - 1$ <table style="border-collapse: collapse; width: 100%;"> <tr> <td style="border-right: 1px solid black; padding: 5px; vertical-align: top;"> $ET \leftarrow 0$ $LT \leftarrow 0$ while $M_{r,3} = 1900 + y \wedge r < \text{rows}(M) - 1$ <table style="border-collapse: collapse; width: 100%;"> <tr> <td style="border-right: 1px solid black; padding: 5px; vertical-align: top;"> $ET \leftarrow ET + 1$ if $M_{r,1} \leq 9$ $LT \leftarrow LT + 1$ otherwise $r \leftarrow r + 1$ $N_{y,0} \leftarrow M_{r-1,3}$ $N_{y,1} \leftarrow ET$ $N_{y,2} \leftarrow LT$ $N_{y,3} \leftarrow ET + LT$ </td> <td style="padding: 5px; vertical-align: top;"> $y \leftarrow y + 1$ </td> </tr> </table> </td> <td style="padding: 5px; vertical-align: top;"> $y \leftarrow y + 1$ </td> </tr> </table>	$ET \leftarrow 0$ $LT \leftarrow 0$ while $M_{r,3} = 1900 + y \wedge r < \text{rows}(M) - 1$ <table style="border-collapse: collapse; width: 100%;"> <tr> <td style="border-right: 1px solid black; padding: 5px; vertical-align: top;"> $ET \leftarrow ET + 1$ if $M_{r,1} \leq 9$ $LT \leftarrow LT + 1$ otherwise $r \leftarrow r + 1$ $N_{y,0} \leftarrow M_{r-1,3}$ $N_{y,1} \leftarrow ET$ $N_{y,2} \leftarrow LT$ $N_{y,3} \leftarrow ET + LT$ </td> <td style="padding: 5px; vertical-align: top;"> $y \leftarrow y + 1$ </td> </tr> </table>	$ET \leftarrow ET + 1$ if $M_{r,1} \leq 9$ $LT \leftarrow LT + 1$ otherwise $r \leftarrow r + 1$ $N_{y,0} \leftarrow M_{r-1,3}$ $N_{y,1} \leftarrow ET$ $N_{y,2} \leftarrow LT$ $N_{y,3} \leftarrow ET + LT$	$y \leftarrow y + 1$	$y \leftarrow y + 1$	$FD := ELF(Hdd)$ $FD_{1907,0} := 1907$ $FD_{1914,0} := 1914$ $\sum FD^{(1)} + \sum FD^{(2)} = 524$ $\text{corr}(FD^{(1)}, FD^{(2)}) = 0.199$ <u>Average # Early & Late</u> $FD_E := \text{mean}(FD^{(1)})$ $FD_L := \text{mean}(FD^{(2)})$ $FD_E = 3.829$ $FD_L = 1.162$
$ET \leftarrow 0$ $LT \leftarrow 0$ while $M_{r,3} = 1900 + y \wedge r < \text{rows}(M) - 1$ <table style="border-collapse: collapse; width: 100%;"> <tr> <td style="border-right: 1px solid black; padding: 5px; vertical-align: top;"> $ET \leftarrow ET + 1$ if $M_{r,1} \leq 9$ $LT \leftarrow LT + 1$ otherwise $r \leftarrow r + 1$ $N_{y,0} \leftarrow M_{r-1,3}$ $N_{y,1} \leftarrow ET$ $N_{y,2} \leftarrow LT$ $N_{y,3} \leftarrow ET + LT$ </td> <td style="padding: 5px; vertical-align: top;"> $y \leftarrow y + 1$ </td> </tr> </table>	$ET \leftarrow ET + 1$ if $M_{r,1} \leq 9$ $LT \leftarrow LT + 1$ otherwise $r \leftarrow r + 1$ $N_{y,0} \leftarrow M_{r-1,3}$ $N_{y,1} \leftarrow ET$ $N_{y,2} \leftarrow LT$ $N_{y,3} \leftarrow ET + LT$	$y \leftarrow y + 1$	$y \leftarrow y + 1$		
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Read Data for Coastal Map of USA and Gulf Regions

```

SwapColumns(M) :=
  N ← M<sup>(1)</sup>          USA := READPRN("World_Map.txt")
  N<sup>(1)</sup> ← M<sup>(0)</sup>   USA := SwapColumns(USA)
  N
  
```

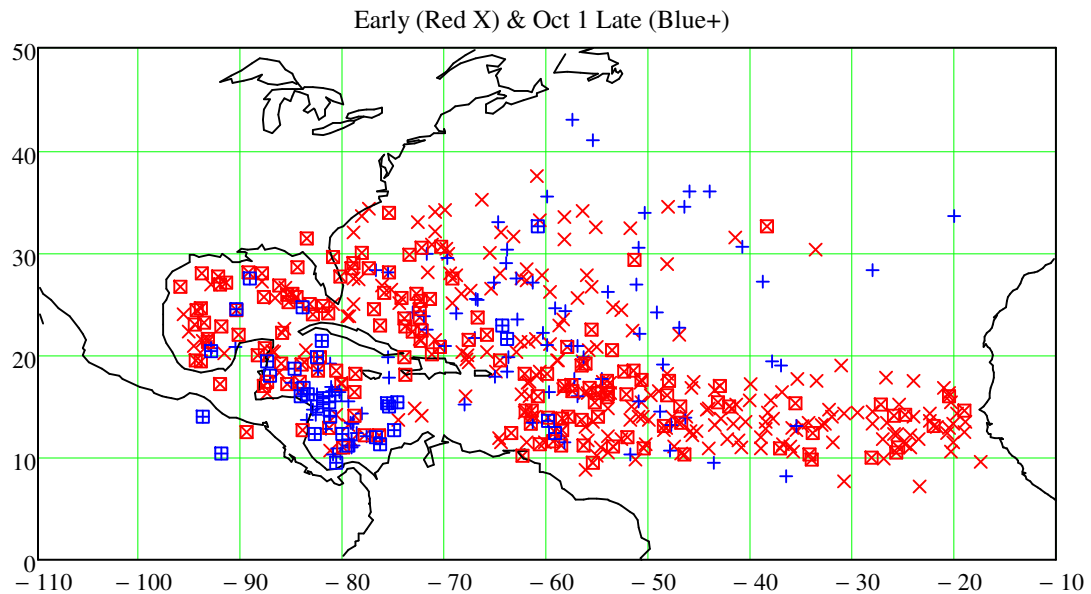
```

PatchJumps(M) :=
  R ← 0
  Nn ← 0
  for r ∈ 0..rows(M) - 2
    Nnr+R,0 ← Mr,0
    Nnr+R,1 ← Mr,1
    if (|Mr,0 - Mr+1,0| > 2) ∨ |Mr,1 - Mr+1,1| > 5
      Nnr+R+1,0 ← Mr,0
      Nnr+R+1,1 ← 106
      R ← R + 1
  Nn
  
```

```

USA := PatchJumps(USA)
  
```

Mark the Start Locations for Hurricanes Making USA Landfall with a box



Accumulated Cyclone Energy - Atlantic

The Atlantic hurricane database (or HURDAT) extends back to 1851
<http://www.aoml.noaa.gov/hrd/tcfaq/E11.html>

The ACE of a season is calculated by summing the squares of the estimated maximum sustained velocity of every active tropical storm (wind speed 35 knots (65 km/h) or higher), at six-hour intervals. If any storms of a season happen to cross years, the storm's ACE counts for the previous year.[2] The numbers are usually divided by 10,000 to make them more manageable. The unit of ACE is 104 kn², and for use as an index the unit is assumed. Thus:

$$ACE = 10^{-4} \sum v_{max}^2 \quad \text{where } v_{max} \text{ is estimated sustained wind speed in knots.}$$

ACE := READPRN("Atlantic Accumulated Cyclone Energy 1851 - 2011.txt")

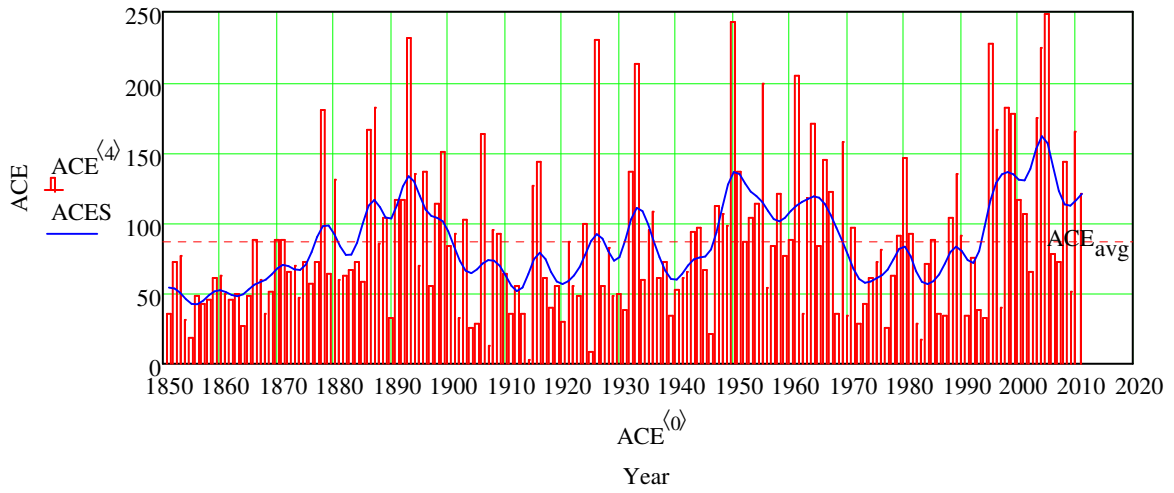
Format: Year Named Storms Hurricanes Major Hurricanes ACE

ACES := ksmooth(ACE⁽⁰⁾, ACE⁽⁴⁾, 5) ACE_{avg} := mean(ACE⁽⁴⁾)

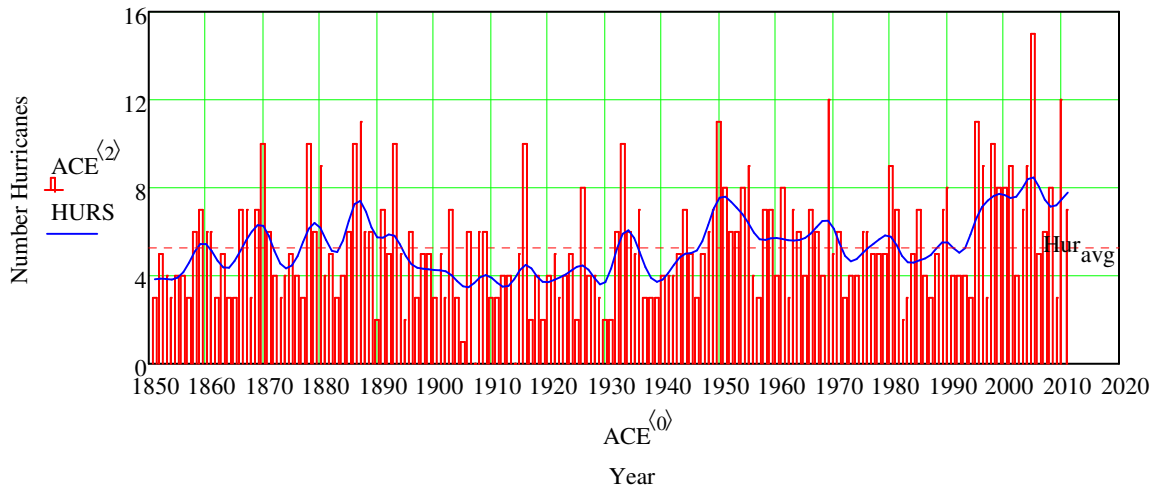
HURS := ksmooth(ACE⁽⁰⁾, ACE⁽²⁾, 5) Hur_{avg} := mean(ACE⁽²⁾)

MHURS := ksmooth(ACE⁽⁰⁾, ACE⁽³⁾, 5) MHur_{avg} := mean(ACE⁽³⁾)

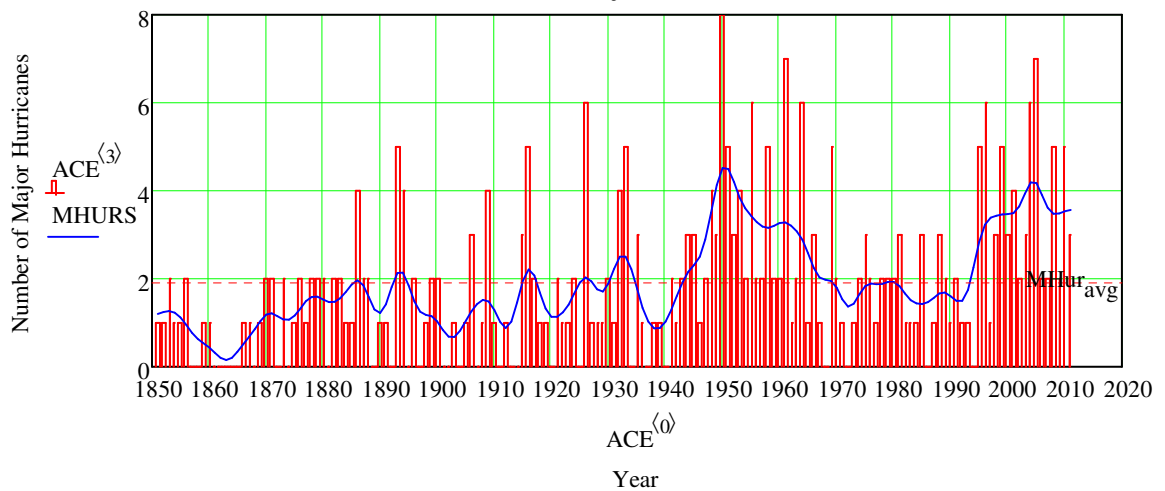
Atlantic Accumulated Cyclone Energy 1850 to 2011. Note Peak in 2005



Atlantic Number of Hurricanes 1850 to 2011



Atlantic Number of Major Hurricanes 1850 to 2011



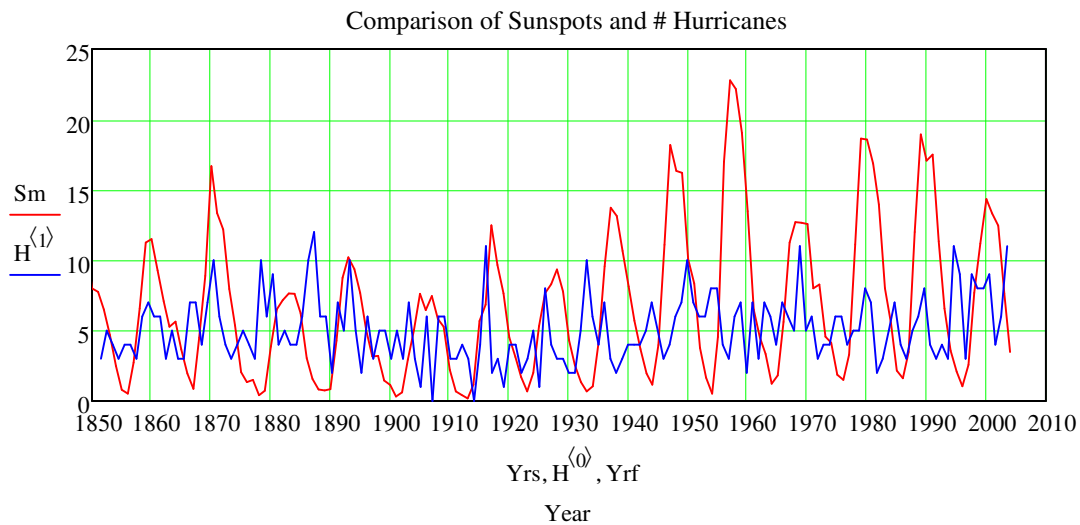
The following data shows that, contrary to most years, the most historically significant climatic factors are not correlated to 2004 season hurricane activity

No Correlation between Sunspot Activity and Hurricanes
Load Sunspot data from 1749 to 2004

SM :=
sunspot_num2.txt

Ry := 2004 - 1749 Ry = 255 r := 0..Ry Yrs_r := 1749 + r

$$V_r^{(1)} := \text{vlookup}(Yrs_r, SM, 2) \quad Sm_r := \frac{1}{100} \cdot \sum V_r^{(1)}$$



No Correlation Sunspots to Frequency of All Hurricanes

Subset of Sunspot Data from 1851 to 2004

Ss := submatrix(Sm, 102, rows(Sm) - 1, 0, 0) Yrs_102 = 1851

$$\text{corr}(Ss, H^{(1)}) = 0.058$$

No Correlation Sunspots to Early and Late Hurricanes

Subset of Sunspot Data from 1900 to 2004

Ss2 := submatrix(Sm, 151, 255, 0, 0) Yrs_151 = 1900
Ss3 := submatrix(Sm, 201, 251, 0, 0)

$$\text{corr}(Ss2, FD^{(1)}) = 0.038$$

$$\text{corr}(Ss2, FD^{(2)}) = 0.087$$

Correlation between El Nino Southern Oscillation and Early, Late and All Hurricanes
Load El Nino data from 1950 to June 2004 (Minus "LastYrs")

Correlate from with ENSO May to Nov Data

http://www.cpc.ncep.noaa.gov/products/analysis_monitoring/ensostuff/ensoyears.html

```

LastYrs := 0      ENSO := READPRN("ENSO Years.txt")      rows(ENSO) = 55

ENSO := submatrix(ENSO, 0, 54 - LastYrs, 5, 11)
r := 0..54 - LastYrs      ENSOT_r :=  $\sum (ENSO^T)^{\langle r \rangle}$       Zero := 0

FD50 := submatrix(FD, 50, 104 - LastYrs, 0, 3)      rows(FD) = 105
    
```

Correlation El Nino and Early

$\text{corr}(ENSO^T, FD50^{\langle 1 \rangle}) = -0.34$

Correlation El Nino and Late

$\text{corr}(ENSO^T, FD50^{\langle 2 \rangle}) = -0.222$

Correlation El Nino and ALL

$\text{corr}(ENSO^T, FD50^{\langle 3 \rangle}) = -0.387$

Better Correlation to BEST (Bivariate ENSO Time Series)

Load BEST data from 1871 to Aug 2004 (Minus "LastYrs")

Correlate from with BEST June to August Data

<http://www.cdc.noaa.gov/people/cathy.smith/best/#values>

```

BEST := READPRN("Best enso_ts_1mn.txt")      rows(BEST) = 134

BEST := submatrix(BEST, 79, 133 - LastYrs, 6, 8)

BESTT_r :=  $\sum (BEST^T)^{\langle r \rangle}$ 
    
```

Correlation BEST and Early

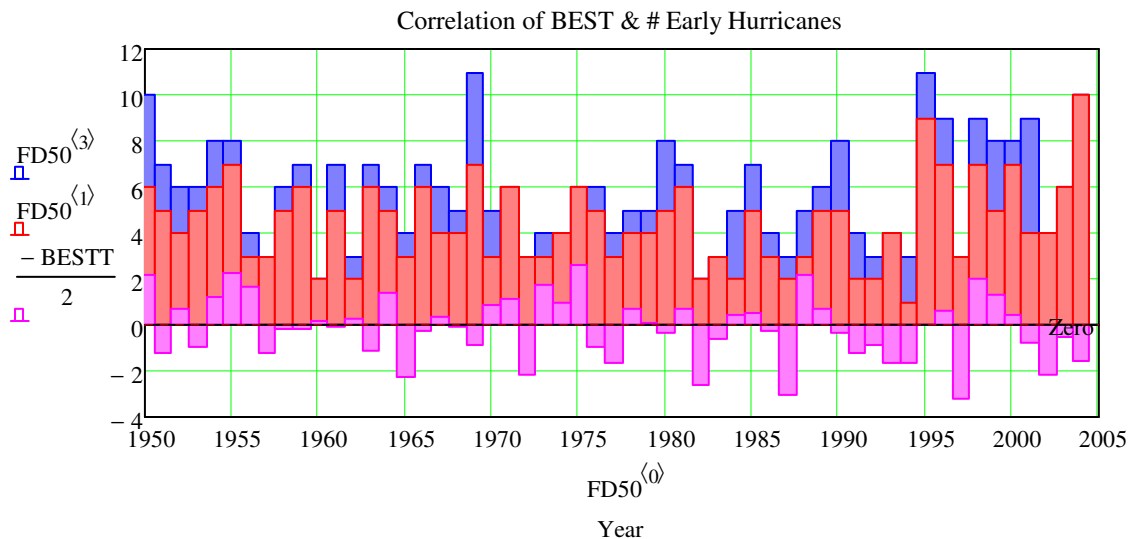
$\text{corr}(BESTT, FD50^{\langle 1 \rangle}) = -0.301$

Correlation BEST and Late

$\text{corr}(BESTT, FD50^{\langle 2 \rangle}) = -0.238$

Correlation BEST and All

$\text{corr}(BESTT, FD50^{\langle 3 \rangle}) = -0.362$



Correlation between Quasi-Biennial Oscillation and Early and Late Hurricanes
Load QBO data from 1948 to August 2004 (Minus "LastYrs")
Correlate from with QBO June to August Data

QBO := READPRN("tsin QBO.txt") rows(QBO) = 57

QBO := submatrix(QBO, 2, 56 - LastYrs, 6, 8)

$$QBOT_r := \sum (QBOT^T)^{\langle 1 \rangle}$$

Correlation QBO and Early

$\text{corr}(QBOT, FD50^{\langle 1 \rangle}) = 0.354$

Correlation QBO and Late

$\text{corr}(QBOT, FD50^{\langle 2 \rangle}) = -0.059$

Correlation QBO and All

$\text{corr}(QBOT, FD50^{\langle 3 \rangle}) = 0.258$

Correlation to Composite of BEST minus QBO versus Early and All

$$BEST_QBO := \left(\frac{BESTT}{\text{mean}(ENSOT)} - \frac{QBOT}{\text{mean}(QBOT)} \right)$$

$\text{corr}(BEST_QBO, FD50^{\langle 1 \rangle}) = 0.348$

$\text{corr}(BEST_QBO, FD50^{\langle 3 \rangle}) = 0.395$

